

Answer the following questions. Each question counts 10 points.

Calculators are not allowed

1. (a) Solve the inequality: $\frac{x^2 - 3x - 4}{|x| - 1} \geq 0$.

(b) Find the equation of the circle passing through the origin and its center is the point of the intersection of the two lines:

$$x + y - 2 = 0 \quad \& \quad x - 2y = -4.$$

2. (a) Let $f(x) = \sqrt{x^2 - 16}$ and $g(x) = \sqrt{3 - x}$.

Find $f \circ g(x)$ and its domain.

(b) Let $f(x) = \begin{cases} |x^2 - 4| & \text{if } x < 2 \\ x - 2 & \text{if } x \geq 2 \\ x + 2 & \text{if } x \geq 2 \end{cases}$

Evaluate $\lim_{x \rightarrow 2} f(x)$ (if exists).

3. (a) Use the definition of limit to prove that $\lim_{x \rightarrow -2} (7x + 2) = -12$.

(b) Evaluate:

$$\lim_{x \rightarrow 3} \left((x - 3)^2 \cos \left(\frac{1}{x - 3} \right) \right).$$

4. (a) Solve the following equation for $\theta \in [0, 2\pi)$:

$$(2 \cos \theta + 1)(\cos \theta - 3) = 0$$

(b) Verify that: $\frac{\sec x - \cos x}{2 \sin^2 x + \cos 2x} = \tan x \sin x$.

GOOD LUCK